Common Symobls

n = Sample Size N = Population Size $\bar{x} =$ Sample Mean $\mu = Population Mean$ s = Sample Standard Deviation σ = Population Standard Deviation $s^2 = Sample Variance$ σ^2 = Population Variance $\hat{p} =$ Sample Proportion p = Population Proportion r = Sample Correlation Coefficient ρ = Population Correlation Coefficient $\alpha = P(Type I error)$ No Yes Is o known? Use the $z_{\alpha/2}$ values

and o in the formula.*

Use the $t_{\alpha/2}$ values and s in the formula.*

*If n < 30, the variable must be normally

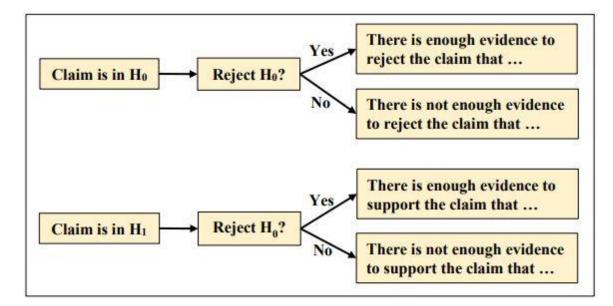
Look for these k	ey words to help	p set up your h	ypotheses:
------------------	------------------	-----------------	------------

Two-tailed Test	Right-tailed Test	Left-tailed Test	
$H_0: \mu = \mu_0 H_1: \mu \neq \mu_0$	$H_0: \mu = \mu_0 H_1: \mu > \mu_0$	$H_0: \mu = \mu_0 H_1: \mu < \mu_0$	
	Claim is in the Null Hypothesis		
=	VI	2	
Is equal to	Is less than or equal to	Is greater than or equal t	
Is exactly the same as	exactly the same as Is at most		
Has not changed from	Is not more than	Is not less than	
Is the same as	Within		
C	aim is in the Alternative Hypoth	esis	
≠	>	<	
Is not	More than	Less than	
Is not equal to	Greater than	Below	
Is different from	Above	Lower than	
Has changed from	Higher than	Shorter than	
Is not the same as	Longer than	Smaller than	
	Bigger than	Decreased	
	Increased	Reduced	

The rejection rule:

- p-value method: reject H₀ when the p-value ≤ α.
- Critical value method: reject H₀ when the test statistic is in the critical tail(s).
- Confidence Interval method, reject H₀ when the hypothesized value found in H₀ is outside the bounds of the confidence interval.

1



One Sample Tests:

Means

 $\begin{array}{l} H_0: \mu = \mu_0 \\ H_1: \mu \neq \mu_0 \end{array} \quad \text{Test statistic when } \sigma \text{ is given in the problem: } z = \frac{\overline{x} - \mu_0}{\left(\sigma / \sqrt{n}\right)} \end{array}$

Test statistic when σ is unknown: $t = \frac{\overline{x} - \mu_0}{(s/\sqrt{n})}$ with df= n - 1

Calculator Short Cut: Press the [STAT] key, go to the [TESTS] menu, arrow down to either the [Z-Test] or [t-test] option and press the [ENTER] key. Arrow over to the [Stats] menu and press the [ENTER] key. Then type in value

for the hypothesized mean (μ_0),standard deviation, sample mean, sample size, arrow over to the \neq , <, > sign that is in the alternative hypothesis statement then press the [ENTER] key, arrow down to [Calculate] and press the [ENTER] key. The calculator returns the test statistic and p-value.

Or (If you have raw data in a list) Select the [Data] menu and press the [ENTER] key. Then type in the value for the hypothesized mean (μ₀), type in your list name (TI-84 L₁ is above the 1 key) (TI-89 list names are in the main folder under Var-Link), leave Freq:1 alone, arrow over to the ≠, <, > sign that is in the alternative hypothesis statement then press the [ENTER]key, arrow down to [Calculate] and press the [ENTER] key. The calculator returns the test statistic and the p-value.

Proportions

$$H_0: p = p_0 \\ H_1: p \neq p_0$$
 Test statistic is $z = \frac{\hat{p} - p}{\sqrt{\frac{p \cdot q}{n}}}$ where $\hat{p} = \frac{x}{n}$

Calculator Short Cut: Press the [STAT] key, select the [TESTS] menu, arrow down to the option [1-PropZTest] and press the [ENTER] key. Type in the value for the hypothesized proportion (p₀), X, sample size, arrow over to the ≠, <, > sign that is in the alternative hypothesis statement then press the [ENTER] key, arrow down to [Calculate] and press the [ENTER] key. The calculator returns the test statistic and p-value. Note: sometimes you are not given the X value but a percentage instead. The calculator will give you an error message if you put in a decimal for X or n. For example if p̂ = .22 and n = 124 then .22*124 = 27.28, so use X = 27.



T-Test Inpt:WERE µg:0	Stats
List:Li Freq:I Migno Kas Calculate	≻×s Draw

Variance or Standard Deviation

 $\begin{array}{ll} H_0: \sigma^2 = \sigma_0^2 \\ H_1: \sigma^2 \neq \sigma_0^2 \end{array} \quad \text{or} \quad \begin{array}{l} H_0: \sigma = \sigma_0 \\ H_1: \sigma \neq \sigma_0 \end{array} \quad \text{Both use test statistic } \chi^2 = \frac{(n-1)s^2}{\sigma_0^2} \text{ with df= n-1.} \end{array}$

Two Sample Tests: 2 Means – Independent Populations

$$\begin{array}{l} H_{0}: \mu_{1} = \mu_{2} \\ H_{1}: \mu_{1} \neq \mu_{2} \end{array} \text{ or } \begin{array}{l} H_{0}: \mu_{1} - \mu_{2} = (\mu_{1} - \mu_{2})_{0} \\ H_{1}: \mu_{1} - \mu_{2} \neq (\mu_{1} - \mu_{2})_{0} \end{array} \text{ where usually you have } \begin{array}{l} H_{0}: \mu_{1} - \mu_{2} = 0 \\ H_{1}: \mu_{1} - \mu_{2} \neq (\mu_{1} - \mu_{2})_{0} \end{array}$$
Test Statistic when σ_{1}^{2} and σ_{2}^{2} are given: $z = \frac{(\overline{x}_{1} - \overline{x}_{2}) - (\mu_{1} - \mu_{2})_{0}}{\sqrt{\frac{\sigma_{1}^{2}}{n_{1}} + \frac{\sigma_{2}^{2}}{n_{2}}}}.$

Press the [STAT] key, select the [TESTS] menu, arrow down to the option [2-SampZTest] and press the [ENTER] key. Arrow
over to the [Data] for raw data in lists or [Stats] menu when stats are already given and press the [ENTER] key. Then type in the
population standard deviations, the first sample mean and sample size, then the second sample mean and sample size, or the list
names for raw data. Arrow over to the ≠, <, > sign that is in the alternative hypothesis statement then press the [ENTER]key,
arrow down to [Calculate] and press the [ENTER] key. The calculator returns the test statistic z and the p-value.

Confidence interval when
$$\sigma_1^2$$
 and σ_2^2 are given: $(\bar{x}_1 - \bar{x}_2) \pm z_{\frac{n}{2}} \sqrt{\left(\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}\right)}$

Press the [STAT] key, arrow over to the [TESTS] (interval on the TI-89) menu, arrow down to the option [2-SampZInt] and press
the [ENTER] key. Arrow over to the [Data] for raw data in lists or [Stats] menu and press the [ENTER] key. Then type in the
population standard deviations, the first sample mean and sample size, then the second sample mean and sample size, then enter
the confidence level. Arrow down to [Calculate] and press the [ENTER] key. The calculator returns the confidence interval.

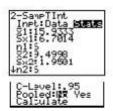
Test statistic when
$$\sigma_1^2$$
 and σ_2^2 are unknown: $t = \frac{(\bar{x}_1 - \bar{x}_2) - (\mu_1 - \mu_2)_0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$

 Press the [STAT] key, arrow over to the [TESTS] menu, arrow down to the option [2-SampTTest] and press the [ENTER] key. Arrow over to the [Data] for raw data in lists or [Stats] menu and press the [Enter] key. Enter the list names or the means, sample standard deviations, sample sizes, and confidence level. Then arrow over to the not equal, <, > sign that is in the alternative hypothesis statement then press the [ENTER] key. Highlight the No option under Pooled for unequal variances. Arrow down to [Calculate] and press the [ENTER] key. The calculator returns the test statistic and the p-value.

with
$$df = \frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}\right)^2}{\left(\left(\frac{1}{n_1 - 1}\left(\frac{s_1^2}{n_1}\right)^2\right) + \left(\frac{1}{n_2 - 1}\left(\frac{s_2^2}{n_2}\right)^2\right)\right)}$$

Confidence interval when σ_1^2 and σ_2^2 are unknown: $(\bar{x}_1 - \bar{x}_2) \pm t_{\frac{n_1}{2}} \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$.

Press the [STAT] key, arrow over to the [TESTS] (interval on the TI-89) menu, arrow down to the
option [2-SampTInt] and press the [ENTER] key. Arrow over to the [Data] for raw data in lists or
[Stats] menu and press the [Enter] key. Enter the list names or means, sample standard deviations,
sample sizes, and confidence level. Highlight the No option under Pooled for unequal variances.
Arrow down to [Calculate] and press the [ENTER] key. The calculator returns the confidence
interval.



2 Means - Dependent Populations

Find the difference (d) between each matched pairs.

$$H_0: \mu_D = 0$$

$$H_1: \mu_D \neq 0$$
Test statistic: $t = \frac{\overline{d} - \mu_0}{\left(\frac{s_d}{\sqrt{n}}\right)}$

Type the data for group1 in L₁ and group 2 in L₂. Arrow up so that you are highlighted on the label of L₃. Then subtract the two lists L₁ - L₂. This puts the differences into L₃ (or just type the differences into a list). In the [STAT] menu, arrow over to the [TESTS] menu, arrow down to the option [T -Test] and press the [ENTER] key. Arrow over to the [Data] menu and press the [ENTER] key. Then type in the hypothesized mean as 0, List: L₃, leave Freq:1 alone, arrow over to the ≠, <, > sign that is the same in the problems alternative hypothesis statement then press the [ENTER]key, arrow down to [Calculate] and press the

[ENTER] key. The calculator returns the t-test statistic, the p-value, $\overline{x} = \overline{d}$ and $S_x = S_D$.

Confidence Interval:
$$\overline{d} \pm t_{q_2} \left(\frac{s_d}{\sqrt{n}} \right)$$
 with df= n - 1.

Type the data for group1 in L₁ and group 2 in L₂. Arrow up so that you are highlighted on the label of L₃. Then subtract the two lists L₁ - L₂. This puts the differences into L₃ (or just type the differences into a list). In the [STAT] menu, arrow over to the [TESTS] (interval on the TI-89) menu, arrow down to the [T-Interval] option and press the [ENTER] key. Arrow over to the [Data] menu and press the [ENTER] key. Type in the List: L₃, Freq:1, and the confidence level. Arrow down to [Calculate] and press the [ENTER] key. The calculator returns the confidence interval, x̄ = d̄ and S_x = S_D.

2 Proportions

$$\begin{array}{l} H_{0}: p_{1} = p_{2} \\ H_{1}: p_{1} \neq p_{2} \end{array} \quad \text{Test statistic } z = \frac{(\hat{p}_{1} - \hat{p}_{2}) - (p_{1} - p_{2})_{0}}{\sqrt{\hat{p}\hat{q}\left(\frac{1}{n_{1}} + \frac{1}{n_{2}}\right)}}, \text{ (usually } (p_{1} - p_{2})_{0} = 0 \text{) where } \hat{p} = \frac{x_{1} + x_{2}}{n_{1} + n_{2}}, \ \hat{q} = 1 - \hat{p} \\ \sqrt{\hat{p}\hat{q}\left(\frac{1}{n_{1}} + \frac{1}{n_{2}}\right)} \end{array}$$

 Press the [STAT] key, arrow over to the [TESTS] menu, arrow down to the option [2-PropZTest] and press the [ENTER] key. Type in the X₁, n₁, X₂, n₂, arrow over to the ≠, <, > sign that is in the alternative hypothesis statement then press the [ENTER] key, arrow down to [Calculate] and press the [ENTER] key. The calculator returns the z-test statistic and the p-value. Note X₁ and X₂ need to be a whole number, not a decimal.

Confidence Interval:
$$(\hat{p}_1 - \hat{p}_2) \pm z_{\frac{q}{2}} \sqrt{\frac{\hat{p}_1(1 - \hat{p}_1)}{n_1} + \frac{\hat{p}_2(1 - \hat{p}_2)}{n_2}}$$
 where $\hat{p}_1 = \frac{x_1}{n_1}$, $\hat{p}_2 = \frac{x_2}{n_2}$.

Press the [STAT] key, arrow over to the [TESTS] menu, arrow down to the option [7:2-PropZInterval] and press the [ENTER] key. Type in the X₁, n₁, X₂, n₂, the confidence level, then press the [ENTER] key, arrow down to [Calculate] and press the [ENTER] key. The calculator returns the confidence interval.

2 Variances or Standard Deviations

$$\begin{array}{ll} H_0:\sigma_1^2 = \sigma_2^2 \\ H_1:\sigma_1^2 \neq \sigma_2^2 \end{array} \quad \text{or} \quad \begin{array}{l} H_0:\sigma_1 = \sigma_2 \\ H_1:\sigma_1 \neq \sigma_2 \end{array} \quad \text{Both use test statistic } F = \frac{s_1^2}{s_2^2} \text{ with dfN} = n_1 - 1 \text{ and dfD} = n_2 - 1. \end{array}$$

 Press the [STAT] key, arrow over to the [TESTS] menu, arrow down to the option [2-SampFTest] and press the [ENTER] key. Arrow over to the [Stats] menu and press the [Enter] key. Then type in the s₁, n₁, s₂, n₂, arrow over to the ≠, <, > sign that is the same in the problems alternative hypothesis statement then press the [ENTER] key, arrow down to [Calculate] and press the [ENTER] key. The calculator returns the test statistic F and the p-value.

Goodness of Fit Test

"There is no preference" w/4 groups H₀: $p_1=.25$, $p_2=.25$, $p_3=.25$, $p_4=.25$ "There is not a preference" H₁: At least one proportion is different. "There is a preference"

Proportions are 1/k or different percentages for each group given in the problem. If %'s are given use those decimals for each p_i . Expected values are found by taking each group's proportion times the sample size ($p_i \times n$),

df=k-1. Test statistic:
$$\chi^2 = \sum \frac{(O-E)^2}{E}$$

- For the TI-84: Enter the observed frequencies in List1, the expected frequency in List2, press [STAT] key, arrow over to [TESTS] menu, arrow down to [χ^2 GOF-Test] (not available on the TI-83 and some TI-84 calculators)
- For the TI-89: Hypothesis test for three or more proportions (goodness of fit test). Go to the [Apps] Stat/List Editor, then type in the observed values into list 1, and the expected values into list 2. Select 2nd then F6 [Tests], then select 7: Chi-2GOF. Type in the list names and the degrees of freedom (df = k-1). Then press the [ENTER] key to calculate. The calculator returns the χ^2 -test statistic and the p-value.

Chi-square Go	odness of Fit
Observed List:	list1
Expected List:	Wet2
Deg of Freedoms dfs	9
R esuits:	Colculate >
Enter=OK	ESC=CANCEL

1:

MATH (200) 234

MATR[X[A] 2 ×4

1,2=0

Test

Observed:[A] Expected:[B] Calculate Dr

Test for Independence

- H0: Variable 1 is independent of Variable 2
- H1: Variable 1 is dependent of Variable 2

Expected values are found by taking $\frac{(\text{Row Total}) \cdot (\text{Column Total})}{\text{Grand Total}}$ for each cell.

Test statistic: $\chi^2 = \sum \frac{(O - E)^2}{E}$.

For the TI-83 or TI-84: Press the [2nd] then [MATRX] key. Arrow over to the EDIT menu and 1:[A] should be highlighted, press the [ENTER] key. For a m X n contingency table, type in the number of rows(m) and the number of columns(n) at the top of the screen so that it looks like this MATRIX[A] m X n. For example a 2 X 3 contingency table, the top of the screen would look like this MATRIX[A] 2 X 4, as you hit [ENTER] the table will automatically widen to the size you put in. Now enter all of the observed values in there proper positions. Then press the [STAT] key, arrow over to the [TESTS] menu,

arrow down to the option [χ^2 -Test] and press the [ENTER] key. Leave the default as Observed: [A] and

Expected:[B], arrow down to [Calculate] and press the [ENTER] key. The calculator returns the χ^2 -test statistic and the p-value. If you go back to the matrix menu [2nd] then [MATRX] key, arrow over to EDIT and choose 2:[B], you will see all of the expected values.

TI-89: First you need to create the matrix for the observed values: Press: [Home] to return to the Home screen, press [Apps] and select 6:Data/Matrix Editor. A menu is displayed, select 3:New. The New dialog box is displayed. Press the right arrow key to highlight 2:Matrix, and press [ENTER] to choose Matrix type. Press the down arrow key to highlight 1:main, and press [ENTER], to choose main folder. Press the down arrow key, and then enter the name o in the Variable field. Enter 3 for Row dimension and 2 for Column dimension. Press [ENTER] to display the matrix editor. Enter 4, 9, 5 in c1 and 7, 2, 3 in c2. Press + [Apps] [ENTER] to close the matrix editor and return to the list editor. If you have more than one Application loaded, press + [Apps], and then select Stats/List Editor .

To display the Chi-square 2-Way dialog box, press 2nd then F6 [Tests], then select 8: Chi-2 2way. Enter in in the Observed Mat: o; Store Expected to: statvars/e; Store CompMat to: statvars/c. This will store the expected values in the matrix folder statvars with the name e, and the (o-e)²/e values in the matrix c. Press the [ENTER] key to calculate. The calculator returns

Observed Mati	matrix1	
Store Expected to:	statuarsie	
Store CompMatto:	statuars\c	
Results:	Calculate >	
Enter=OK >	ESC=CANCEL	

the χ^2 -test statistic and the p-value. If you go back to the matrix menu you will see all of the expected and (o-e)2/e values.

Correlation and Regression

Test statistic for correlation: $t = r \sqrt{\left(\frac{(n-2)}{(1-r^2)}\right)}$ with df= n-2 $H_0: \rho = 0$ $H_1: \rho \neq 0$

 In the [STAT] editor enter the x values into list one and the y values into list two. In the [TESTS] menu, arrow down to the option [LinRegTTest] and press the [ENTER] key. The default is Xlist: L₁, Ylist: L₂, Freq:1, β and $\rho \neq 0$. Arrow down to Calculate and press the [ENTER] key. The calculator returns the t-test statistic, the y-intercept a, slope b, the standard error of estimate s=sest, the coefficient of determination R2, and the correlation coefficient r.

Prediction Interval for a predicted value of y: $\hat{y} \mp t_{\alpha/2} \cdot s_{est} \sqrt{1 + \frac{1}{n} + \frac{n(x - \bar{x})^2}{(n \cdot \Sigma x^2 - (\Sigma x)^2)}}$ with df = n - 2.

$$R_{adj}^2 = 1 - \left(\left(1 - R^2 \left(\frac{n-1}{n-p-1} \right) \right) \right)$$

One-Factor ANOVA table k=#of groups, N=total of all n's

Source	SS	df	MS	F (Test Statistic)
Between (Treatment or Factor)	$SS_B = \Sigma n (\bar{x} - \bar{x}_{GM})^2$	k-1	$MS_B = SS_B / df_B$	$F = MS_B / MS_W$
Within (Error)	$SS_W = \Sigma(n-1)s^2$	N-k	$MS_W = SS_W / df_W$	
Total	SST	N-1		

H₀: $\mu_1 = \mu_2 = \mu_3 = ... = \mu_k$

H1: At least one mean is different CV: Always right-tailed F, use dfN=dfB and dfD=dfw

For the TI-83 or TI-84: Note you have to have the actual raw data to do this test on the calculator. Press the [STAT] key and then the [EDIT] function, type the three lists of data into list one, two and three. Press the [STAT] key, arrow over to the [TESTS] menu, arrow down to the option [F:ANOVA(] and press the [ENTER] key. This brings you back to the regular screen where you should now see ANOVA(. Now hit the [2nd] [L₁][,] [2nd] [L₂] [,][2nd] [L₃][)] keys in that order. You should now see

ANOVA(L_1 , L_2 , L_3), if you had 4 lists you would then have an additional list. Press the [ENTER] key. The calculator returns the F-test statistic, the p-value, Factor (Between) df, SS and MS, Error (Within) df, SS and MS. The last value Sxp is the square root of the MSE.

 For the TI-89: Go to the [Apps] Stat/List Editor, then type in the data for each group into a separate list, (or if you do not have the raw data, enter the sample size, sample mean and sample variance for group 1 into list1 in that order, repeat for list2, etc). Select 2nd then F6 [Tests], then select C:ANOVA. Select the input method data or stats. Select the number of groups. Press the [ENTER] key to calculate. The calculator returns the F-test statistic, the p-value, Factor (Between) df, SS and MS, Error (Within) df, SS and MS. The last value Sxp is the square root of the MSE.

And in case of the local division of the loc	ysis of Yaria	_
List 1: Tat	1	
List 2: Tist	2	
List 3: Tist	3	11

When you reject H_0 for a one-factor ANOVA then you should do a multiple comparison. For example for 3 groups you would have the following 3 comparisons. (4 groups would have $_{4}C_{2}=6$ comparisons)

$H_0:\mu_1=\mu_2$	$H_0:\mu_1=\mu_3$	$H_0:\mu_2=\mu_3$
$H_1:\mu_1\neq\mu_2$	H₁:µ₁≠µ₃	H ₁ :µ2≠µ3

• Scheffé Test Statistic (unequal n): $F_{S} = \frac{\left(\bar{x}_{i} - \bar{x}_{j}\right)^{2}}{\left(MSE\left(\frac{1}{n_{i}} + \frac{1}{n_{j}}\right)\right)}$. Critical Value: (k-1)×(CV from original ANOVA)

• Bonferroni Test $t = \frac{(\bar{x}_i - \bar{x}_j)}{\sqrt{MSE\left(\frac{1}{n_i} + \frac{1}{n_j}\right)}}$ with df = N - k and multiply the p-value by $_kC_2$ groups. For example if

you use the tcdf in your calculator to find the area in both the tails and you have 4 groups you would multiply the tail areas by $_{4}C_{2}=6$.

Two-Factor ANOVA table a=# or row factors, b=# of column factors, n=sample	e size in one group, N=total
--	------------------------------

Source	SS	df	MS	F (3 Test Statistics)
Row (Factor A)	SSA	a-1	$MS_A = SS_A / df_A$	$F_A = MS_A / MS_E$
Column (Factor B)	SSB	b-1	$MS_B = SS_B / df_B$	$F_B = MS_B / MS_E$
Interaction $(A \times B)$	SSA×B	(a-1)(b-1)	$MS_{A\times B} = SS_{A\times B} / df_{A\times B}$	$F_{A\times B} = MS_{A\times B} / MS_{E}$
Error (Within)	SSE	ab(n-1)	$MS_E = SS_E / df_E$	
Total	SST	N-1		
ow Effect (Factor A):	H ₀ : The	e row variable	has no effect on the average	

H1: The row variable has an effect on the average